

Formal Specification and Verification of Fully Asynchronous Implementations of the Data Encryption Standard

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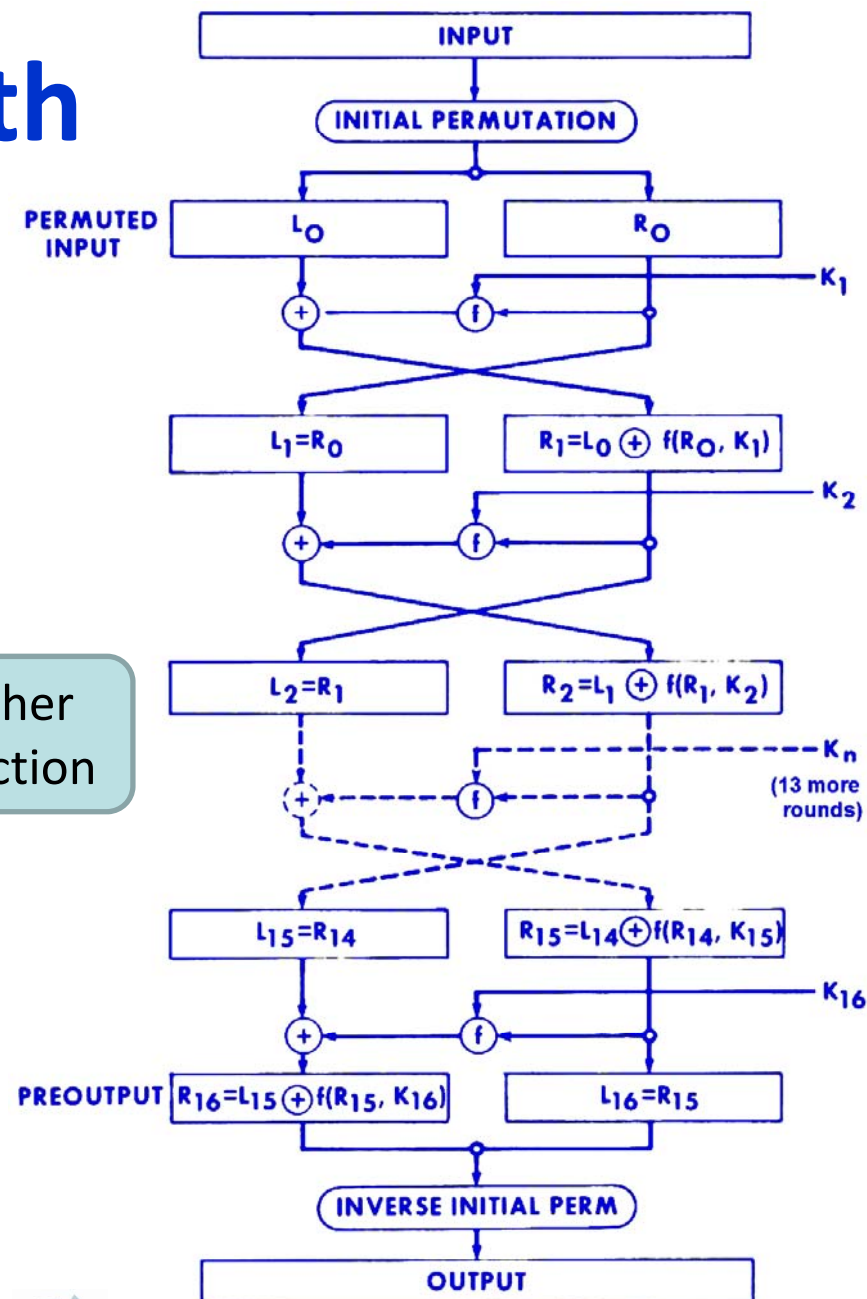
Data Encryption Standard (DES)

- Symmetric-key block cipher
 - ▶ Input: 64-bit data block, 64-bit key, cipher/decipher
 - ▶ Output: (de)ciphered 64-bit data block
- FIPS standard 46 for almost 30 years
- Main weakness: only 56 *useful* key bits
- TDEA (or Triple DES)
 - ▶ approved block cipher (at least until 2030)
 - ▶ recommended for payment systems EMV
 - ▶ three applications of the DES with three different keys:
cipher, decipher, cipher
- Specified as data-flow diagram

DES: Data Path

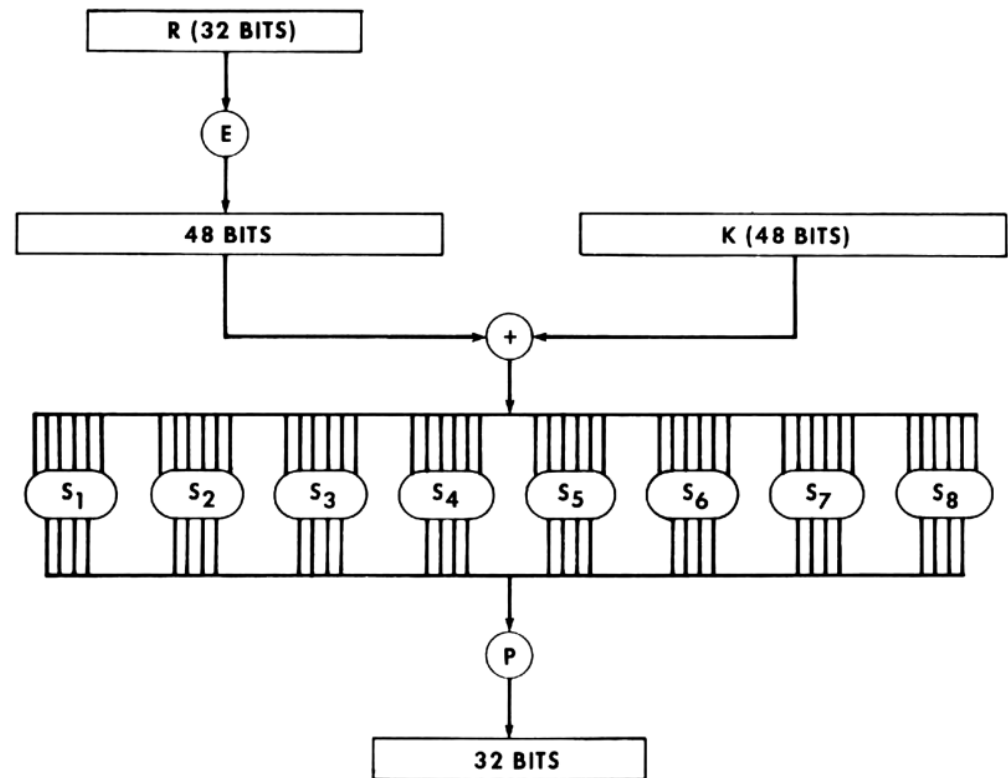
- Permute and split 64-bit data into 32-bit words L_0 and R_0
- iteratively compute:
 $L_i := R_{i-1}$
 $R_i := L_{i-1} \oplus f(R_{i-1}, K_i)$
- return permuted concatenation of R_{16} and L_{15}

cipher function



DES: Cipher Function

- Expand R_{i-1} to 48-bit word E (R_{i-1})
- Split E (R_{i-1}) \oplus K_i into eight 6-bit words $X_1 \dots X_8$
- Compute eight 4-bit words $Y_j := S_j(X_j)$ (using the S-boxes S_j)
- Return permutation of the concatenation $Y_1 \dots Y_8$



DES: Key Path

- select and split 64-bit key into 28-bit words C_0 and D_0

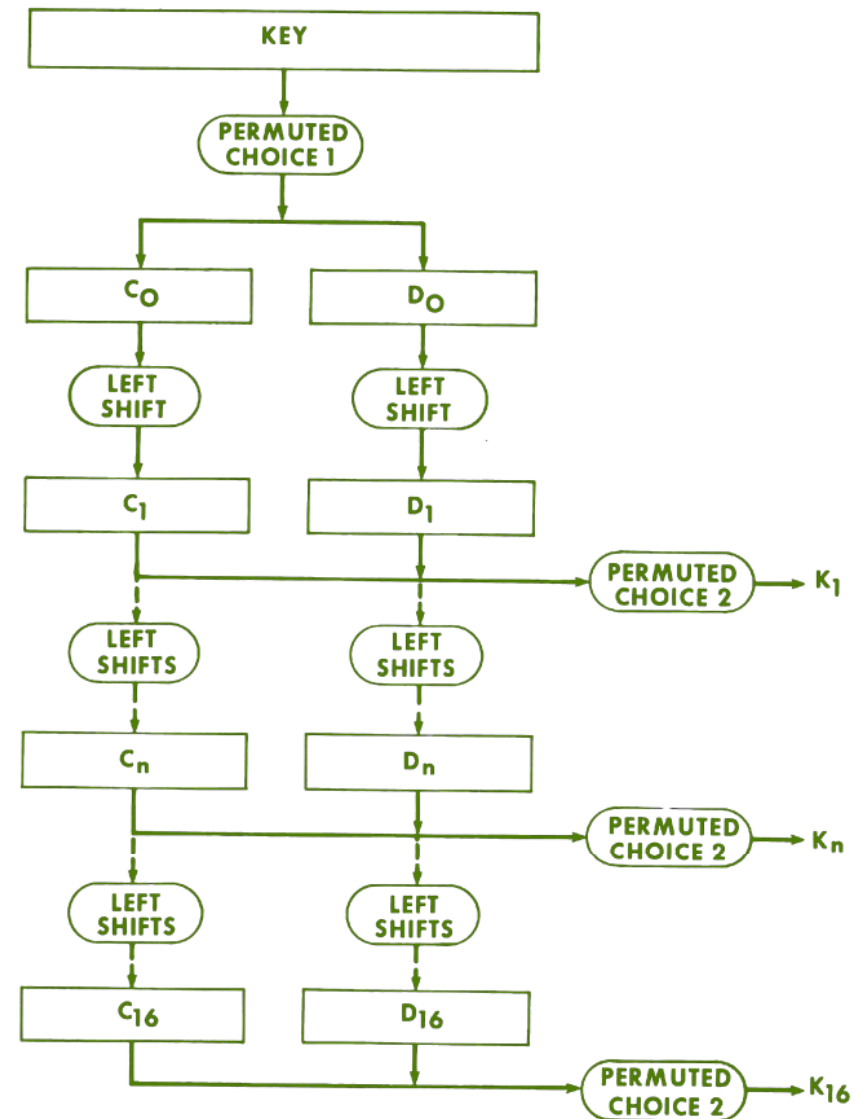
- iteratively compute:

$$C_i := \text{LeftShift}(i, C_{i-1})$$

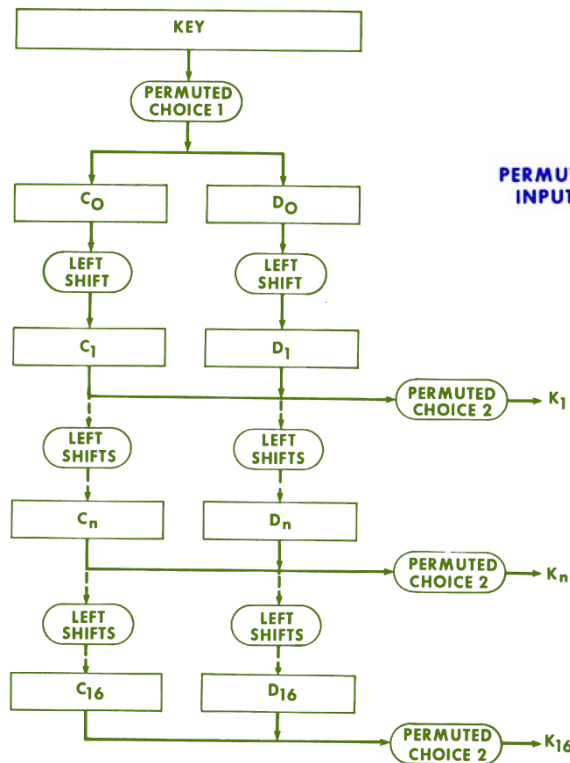
$$D_i := \text{LeftShift}(i, D_{i-1})$$

shift left by 1 or 2 bits
(depending on i)

$K_i :=$ selection of 48 bits
from C_i and D_i

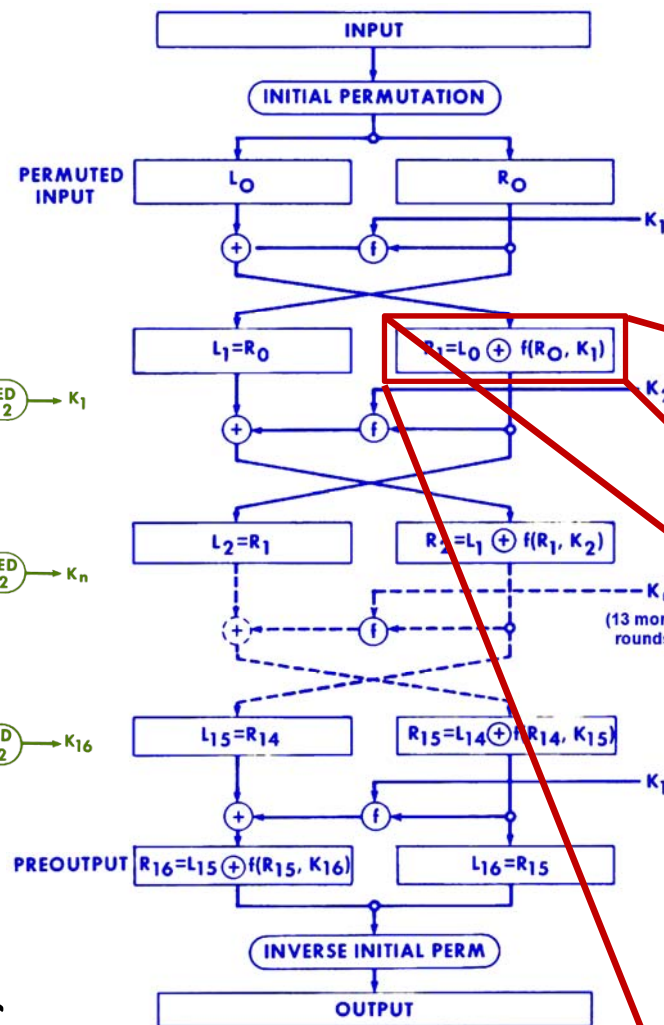


Data-flow Diagram of the DES



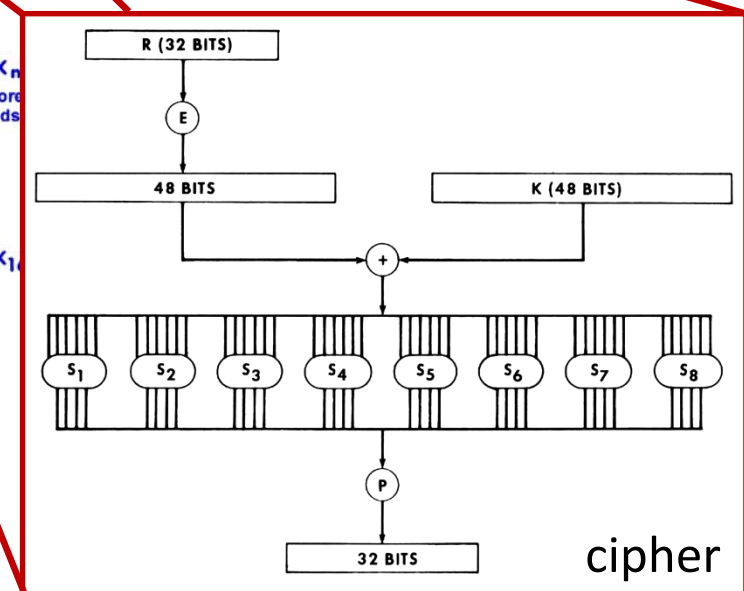
key path

- 16 iterations
- deterministic blocks



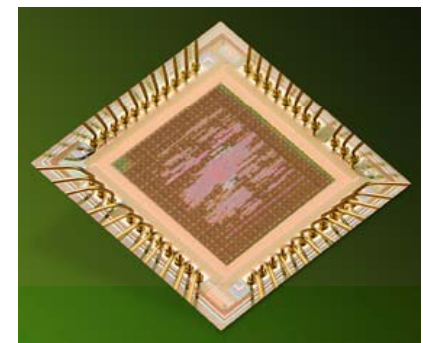
data path

- highly parallel (S-boxes S_i)
- asynchronous
- nondeterministic execution



Related Work

- Asynchronous circuit described in CHP
 - ▶ tolerance of low and variable power supply
 - ▶ low power consumption
 - ▶ resistance to security attacks
(side-channel, fault-injection)
- 2003: Translation of simplified CHP to IF
 - ▶ Generation of the state space (LTS)
 - ▶ Model and equivalence checking (CADP)
- 2008: DES4 chip released



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History of our Models

- 2003: LOTOS model
 - ▶ derived from the DES standard
 - ▶ fully asynchronous
 - ▶ compositional LTS generation and verification
 - ▶ rapid prototyping
- 2004: development of the CHP2LOTOS compiler
 - ▶ application to the CHP model of the DES
 - ▶ improved verification performance compared to IF
- 2015: LNT model
 - ▶ rewrite of the LOTOS model
 - ▶ additional properties

CADP (<http://cadp.inria.fr>)



- Construction and Analysis of Distributed Processes
- *Modular* toolbox with *several*
 - ▶ **Formal specification languages:**
LOTOS, LNT, FSP, π -calculus, ...
 - ▶ **Verification paradigms:**
model checking, equivalence checking, visual checking, ...
 - ▶ **Analysis techniques:**
reachability, on-the-fly, compositional, distributed, static analysis, rapid prototyping, test generation, performance evaluation, ...
- Continuous development for more than 25 years
- More than 150 case-studies and 70 3rd party tools

LOTOS and LNT

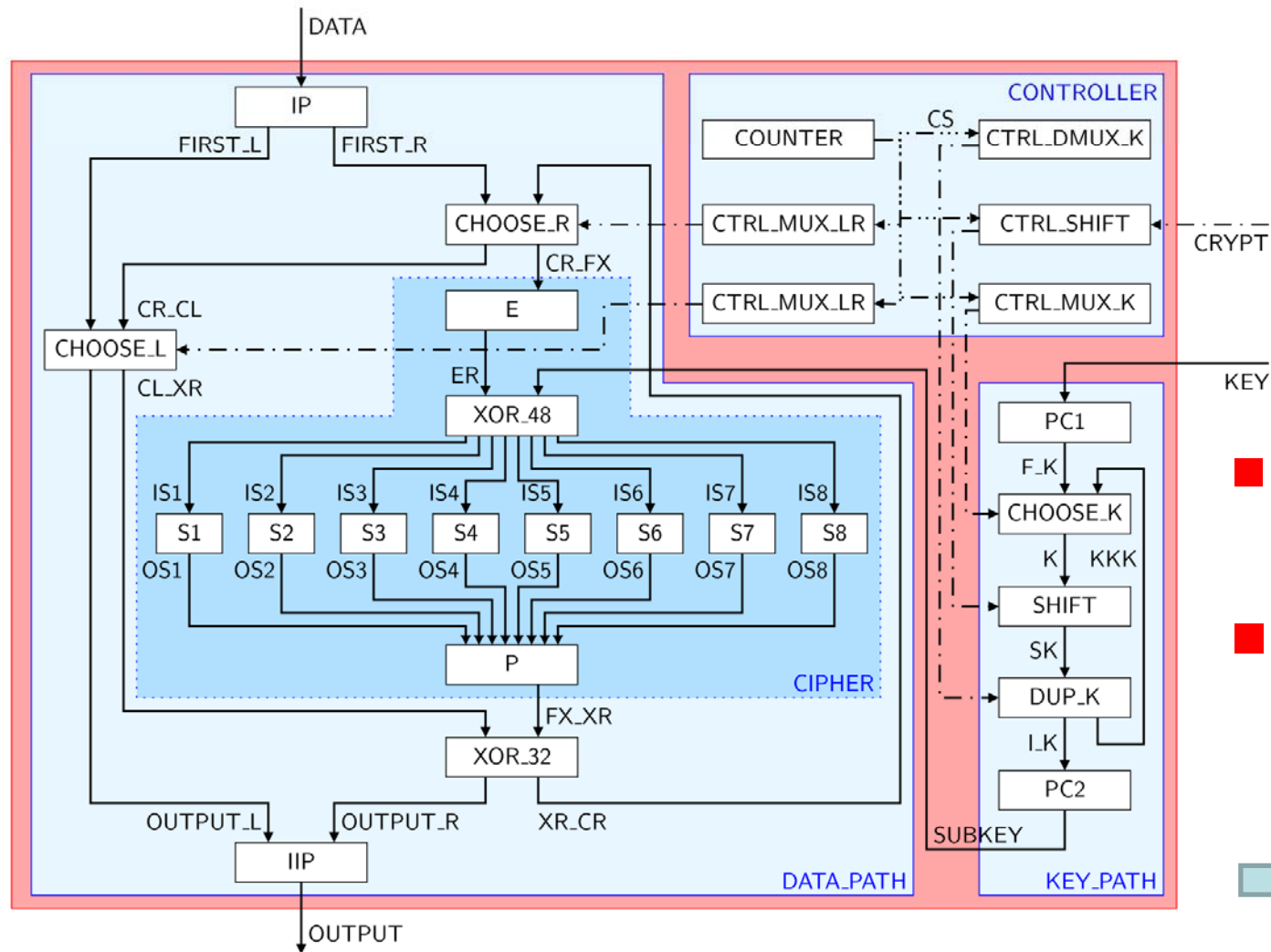
■ LOTOS

- ▶ international standard ISO:8807 (1988)
- ▶ combination of CCS, CSP and abstract data types
- ▶ powerful, but steep learning curve

■ LNT [[Champelovier-Clerc-Garavel-et-al-10](#)]

- ▶ simplification of international standard E-LOTOS
- ▶ *symmetrical* sequential composition
- ▶ process calculus with imperative syntax
- ▶ development partially funded by industry
- ▶ currently implemented by translation into LOTOS

Architecture of the Formal Models



■ correspondence:
block -> process

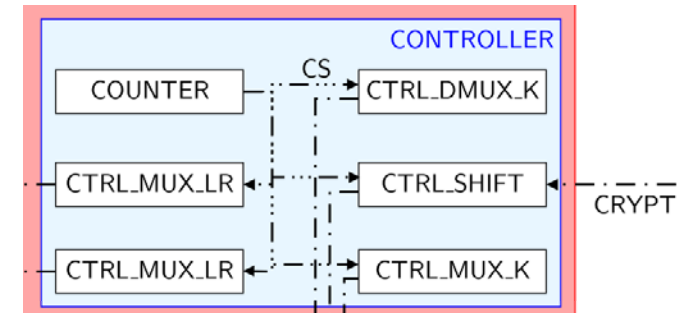
■ share processes
between
iterations

➡ add control
processes &
multiplexers

Six Control Processes

■ Controller for Shift-Register

- ▶ amount (1 or 2 bits) and
- ▶ shift direction (left or right)



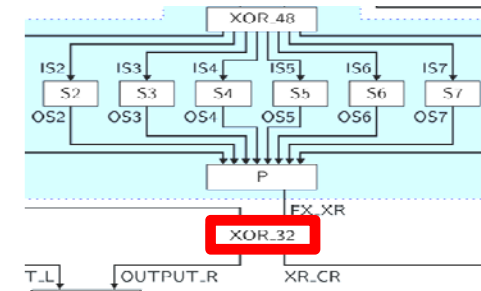
■ Four controllers for multiplexers

- ▶ choice of input: initial value or previous iteration
- ▶ output: next iteration or final result

■ Counter of the iterations: 0 to 16

- ▶ one value more than the number of iterations
- ▶ multiplexers before and after each iteration

Example: XOR_32



```

process XOR_32 [A, B, R: C32] is
  var A32, B32: BIT32 in
    loop
      par
        A (?A32)
        ||
        B (?B32)
      end par;
      R (XOR (A32, B32))
    end loop
  end var
end process -- LNT

```

```

process XOR_32 [A, B, R] : noexit :=
(
  A ? A32 : BIT32;
  exit (A32, any BIT32)
  |||
  B ? B32 : BIT32;
  exit (any BIT32, B32)
)
>> accept A32, B32 : BIT32 in
  R ! XOR (A32, B32);
  XOR_32 [A, B, R]
endproc (* LOTOS *)

```

Example: CIPHER

process CIPHER [K: C48, R, PX: C32] **is**

hide ER: C48,

IS1, IS2, IS3, IS4, IS5, IS6, IS7, IS8: C6,

SO1, SO2, SO3, SO4, SO5, SO6, SO7, SO8: C4 **in**

par

ER ->

E [R, ER]

|| ER, IS1, IS2, IS3, IS4, IS5, IS6, IS7, IS8 ->

XOR_48 [ER, K, IS1, IS2, IS3, IS4, IS5, IS6, IS7, IS8]

|| IS1, IS2, IS3, IS4, IS5, IS6, IS7, IS8, SO1, SO2, SO3, SO4, SO5, SO6, SO7, SO8 ->

par

S1 [IS1, SO1] || S2 [IS2, SO2] || S3 [IS3, SO3] || S4 [IS4, SO4]

|| S5 [IS5, SO5] || S6 [IS6, SO6] || S7 [IS7, SO7] || S8 [IS8, SO8]

end par

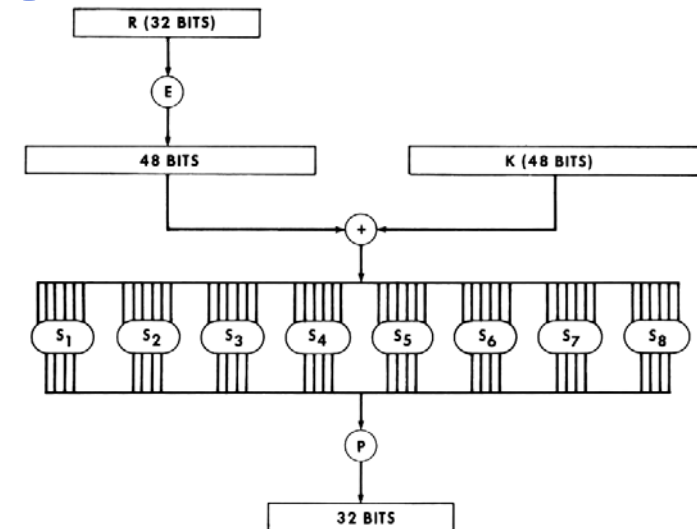
|| SO1, SO2, SO3, SO4, SO5, SO6, SO7, SO8 ->

P [SO1, SO2, SO3, SO4, SO5, SO6, SO7, SO8, PX]

end par

end hide

end process -- LNT



Comparison of LNT and LOTOS Models

	LOTOS	LNT	generated LOTOS
types & functions	1172	575	2514
channels	0	50	58
processes	671	668	772
<i>total</i>	<i>1843</i>	<i>1293</i>	<i>3344</i>

- LNT shorter
- LNT closer to the standard
- generated LOTOS much larger, due to
 - ▶ automatically generated data types (S-boxes matrices)
 - ▶ automatically generated auxiliary functions

S-Boxes in the Standard

■ Compute $S_k(X)$, with $X = B_1B_2B_3B_4B_5B_6$

▶ row $i = B_1B_6$, column $j = B_2B_3B_4B_5$

▶ return binary representation of $S_k[i, j]$

■ Example: $S_1(011011)$

▶ $i = 01 = 1$, $j = 1101 = 13$, $S_1[1, 13] = 5$

▶ $S_1(011011) = 0101$

S_1

		14	4	13	1	2	15	11	8	3	10	6	12	5	9	0	7
$i = 1$		0	15	7	4	14	2	13	1	10	6	12	11	9	5	3	8
		4	1	14	8	13	6	2	11	15	12	9	7	3	10	5	0
		15	12	8	2	4	9	1	7	5	11	3	14	10	0	6	13

$j = 13$

S-Boxes in LNT

type ROW **is** array [0..15] **of** NAT **end type**

type S_BOX_ARRAY **is** array [0..3] **of** ROW **end type**

function GET_ROW (X: BIT6) : NAT **is**

return BIT2_TO_NAT (1AND6 (X))

end function

function GET_COLUMN (X: BIT6) : NAT **is**

return BIT4_TO_NAT (2TO5 (X))

end function

function S1 : S_BOX_ARRAY **is**

return S_BOX_ARRAY

 (ROW (14, 4, 13, 1, 2, 15, 11, 8, 3, 10, 6, 12, 5, 9, 0, 7),

 ROW (0, 15, 7, 4, 14, 2, 13, 1, 10, 6, 12, 11, 9, 5, 3, 8),

 ROW (4, 1, 14, 8, 13, 6, 2, 11, 15, 12, 9, 7, 3, 10, 5, 0),

 ROW (15, 12, 8, 2, 4, 9, 1, 7, 5, 11, 3, 14, 10, 0, 6, 13))

end function

process S1 [INPUT: C6, OUTPUT: C4] **is**

loop var I6: BIT6 **in**

 INPUT (?I6);

 OUTPUT (NAT_TO_BIT4 (S1[GET_ROW (I6)][GET_COLUMN (I6)]))

end var end loop

end process

S-Boxes in LOTOS

type S_BOX_FUNCTIONS is BIT4, BIT6

opns S1 : BIT6 -> BIT4

eqns

ofsort BIT4 **forall** BV6 : BIT6

BV6 = MK_6 (0, 0, 0, 0, 0, 0) => S1 (BV6) = MK_4 (1, 1, 1, 0);

BV6 = MK_6 (0, 0, 0, 0, 1, 0) => S1 (BV6) = MK_4 (0, 1, 0, 0);

BV6 = MK_6 (0, 0, 0, 1, 0, 0) => S1 (BV6) = MK_4 (1, 1, 0, 1);

BV6 = MK_6 (0, 0, 0, 1, 1, 0) => S1 (BV6) = MK_4 (0, 0, 0, 1);

BV6 = MK_6 (0, 0, 1, 0, 0, 0) => S1 (BV6) = MK_4 (0, 0, 1, 0);

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BV6 = MK_6 (0, 0, 1, 1, 1, 0) => S1 (BV6) = MK_4 (1, 0, 0, 0);

[... (54 lines)]

BV6 = MK_6 (1, 1, 1, 1, 0, 1) => S1 (BV6) = MK_4 (0, 1, 1, 0);

BV6 = MK_6 (1, 1, 1, 1, 1, 1) => S1 (BV6) = MK_4 (1, 1, 0, 1);

endtype

process S1 [INPUT, OUTPUT] : **noexit** :=

INPUT ?/6:BIT6;

OUTPUT !S1(/6);

S1 [INPUT, OUTPUT]

endproc

Modeling Results

- Process calculi adapted for asynchronous circuits
- Benefits of rewrite to LNT
 - ▶ correction of minor errors (incorrect S-boxes)
 - ▶ simplified controller (7% fewer lines)
 - ▶ increased asynchronism (accept next CRYPT earlier)
 - ▶ new version of the LOTOS model
 - ▶ correction of a small bug in the LNT2LOTOS translator (support for functions called like numbers, e.g. “1”)

Analysis Challenge

- LTS size: enumeration of 64-bit input data and key
- Two approaches
 - ▶ Data abstraction
 - ▶ Environment constraints

Data Abstraction

■ Abstract Bits to a singleton

▶ bit vector  singleton

▶ operation on bit vector  identity

■ Concrete Bit

type BIT is

0, 1

with "=="

end type

■ Abstract Bit

type BIT is

0

with "=="

end type

function 1 : BIT is

return 0

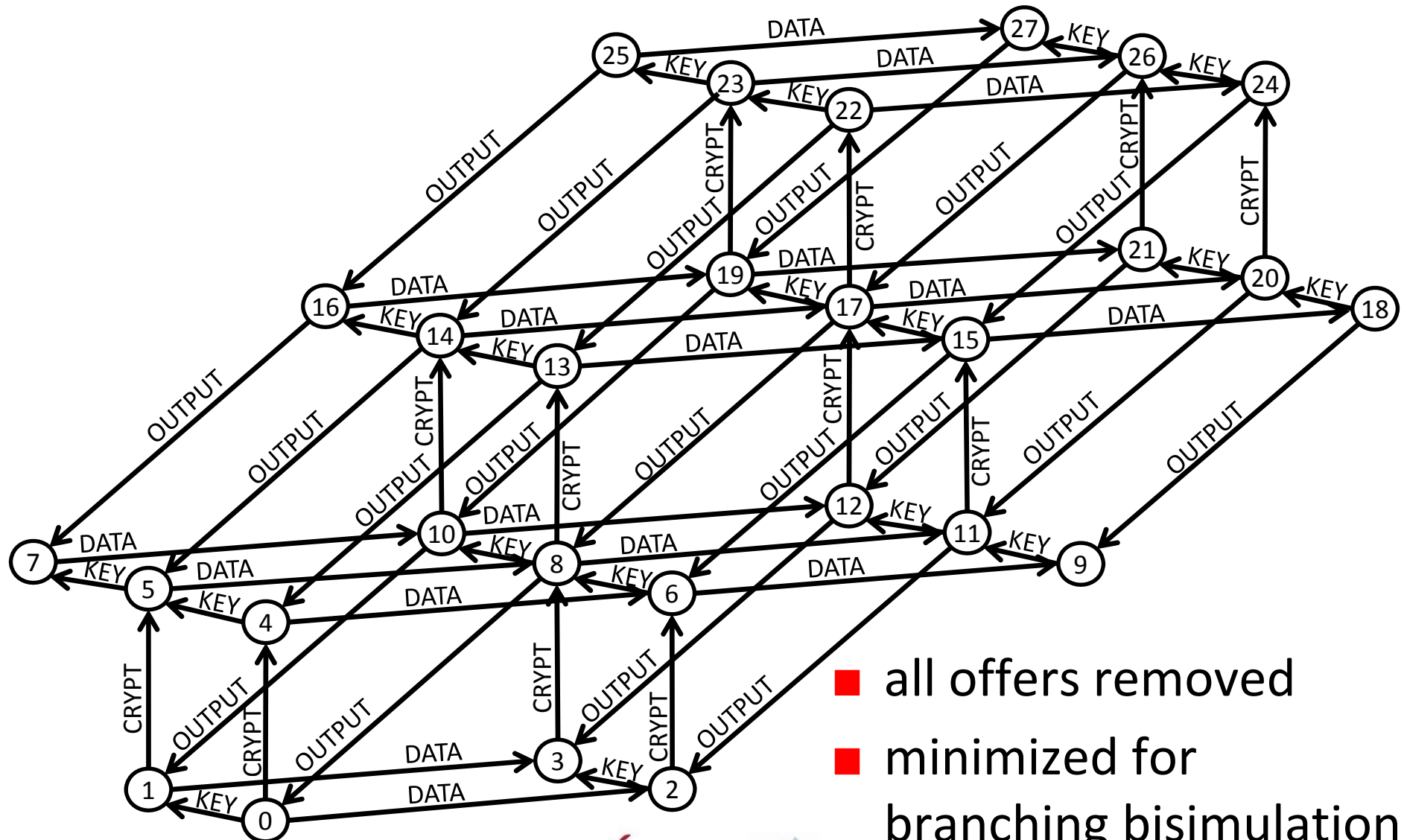
end function

LTS Generation (Abstract Model)

	direct generation		compositional	
	LOTOS	LNT	LOTOS	LNT
states	591,914,192	167,300,852	688,422	406,192
transitions	5,542,917,498	1,500,073,686	5,122,760	2,910,530
time (minutes)	228	66	1.4	1
RAM (GB)	19.13	4.93	0.19	0.11

- Largest intermediate LTS
- Total time (without minimization for direct generation)
- Maximal RAM requirements
- Final LTS of all cases (reduced for branching bisimulation):
28 states, 78 transitions
- Measurements in August 2015 (on a Xeon® E5-2630 @2.4 GHz)

Final Abstract LTS

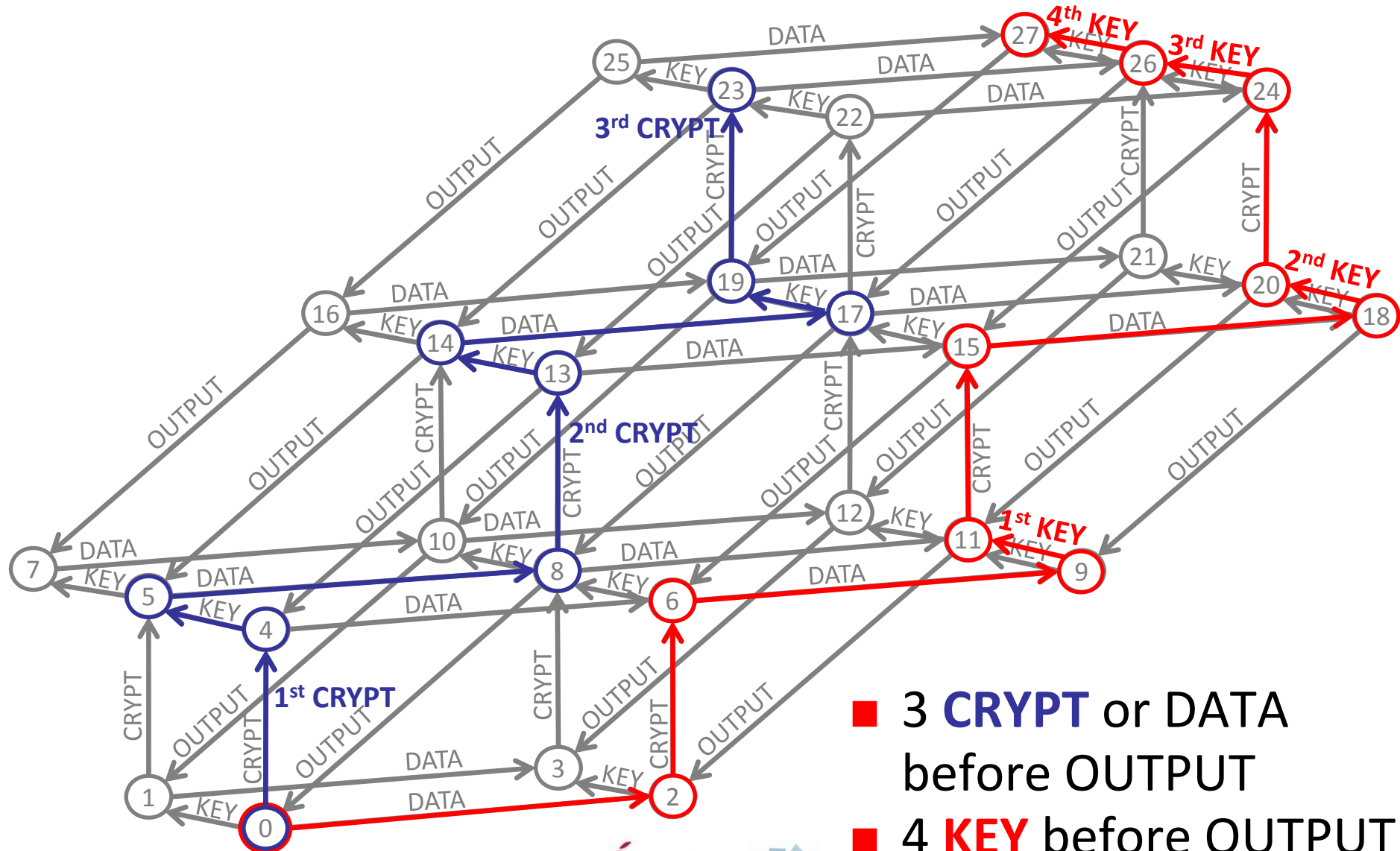


- all offers removed
- minimized for branching bisimulation

Model Checking (Abstract Model)

- Absence of deadlocks
- Triplet of inputs eventually followed by OUTPUT
[**true*** . PARALLEL (CRYPT, DATA, KEY)]
INEVITABLE (OUTPUT)
- Acceptance of n inputs A in advance
 - ▶ never accept more than n inputs A in advance
[**true*** . (A . **not** (A or OUTPUT)*) $\{n\}$. A] **false**
 - ▶ there exists an execution with n inputs in advance
< **true*** . (A . **not** (A or OUTPUT)*) $\{n-1\}$. A > **true**
 - ▶ note: n varies for the three inputs

Examples of Inputs in Advance

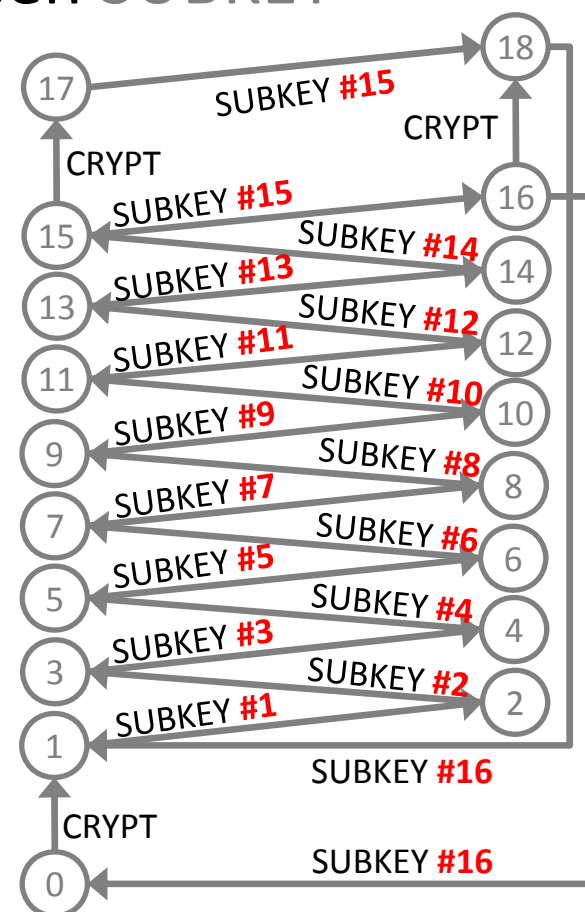


- 3 **CRYPT** or DATA before OUTPUT
- 4 **KEY** before OUTPUT

Equivalence Checking (Abstract Model)

- Correct synchronization of data and key paths
“sixteen SUBKEY times between two CRYPT, and
CRYPT may not happen before fourteen SUBKEY”

- `"des_crypt_subkey.bcg"` =
**branching reduction of
total rename**
 `"CRYPT.*" -> CRYPT,`
 `"SUBKEY.*" -> SUBKEY in`
hide DATA, OUTPUT, KEY in
 `"des.bcg";`
branching comparison
 `"property_4.Int" ==`
 `"des_crypt_subkey.bcg";`



Direct Generation (Concrete Model)

■ Environment

- ▶ provide input: data, key, operation mode
- ▶ check output

■ Several possibilities: collateral, sequential, ...

■ Results

- ▶ correct output
[not ({ OUTPUT ... }) *] INEVITABLE ({ OUTPUT ... })
- ▶ without offers, LTS included in the final abstract LTS

Rapid Prototyping

- EXEC/CAESAR framework
- Visible rendezvous = call to a gate function (in C)
 - ▶ data exchange with environment (read input, output)
 - ▶ accept/refuse rendezvous
- Interaction via standard input and standard output
- One line per rendezvous (LOTOS syntax)

```
CRYPT !1  
DATA !0123456789abcdef  
KEY !133457799bbcdff1
```

- Signal mismatch
(unexpected rendezvous)

```
$ ./des  
CRYPT !1  
DATA !0123456789abcdef  
KEY !133457799bbcdff1  
KEY !133457799bbcdff1  
CRYPT !0  
DATA !85e813540f0ab405  
OUTPUT !85e813540f0ab405  
CRYPT !1  
KEY !133457799bbcdff1  
DATA !0123456789abcdef  
OUTPUT !0123456789abcdef
```

Conclusion

■ Challenging Benchmark

- ▶ large, but tractable
- ▶ experimentation with various techniques



distributed generation

- Ease of data abstraction in process calculi
- Rapid prototyping from formal models
- Complete models and verification scenario

http://cadp.inria.fr/demos/demo_38

